

Student ID :

Name :

**Theory of Computation final exam (2017-2018 Fall)**

*(Please use free space for draft and fit your answer to boxes.)*

1. (25P) Prepare Chomsky normal form of  $A \rightarrow aA \mid Ad \mid B$ ,  $B \rightarrow bBc \mid b$

2. (25P) Design such a Turing machine that writes letter "c"s to the second tape as much as  $|a|^{|b|}$ . Here,  $|a|$  is the number of "a"s and  $|b|$  is the number of "b"s in the first tape. For example, if the user enters "aabb" in the first tape, the Turing code writes "cccccc" into the second tape because of  $2^3$  (the number of "a"s is 2 and the number of "b"s is 3) computation.

3. (25P) Assume that any electrical car in the world can run infinite time. When we want to prepare a software to compute the total road amount (as distance) where all electrical cars in the world can go, how can we comment this software in terms of decidability?

4. (25P) Describe a transform 3SAT problem into 3COLORING with an algorithm in polynomial time.