

Student ID :
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Automata Theory Course Quiz-2 (2016-2017Fall)
(Please use free space for draft and fit your answer to boxes.)

1. (50P) Find whether given grammar can produce "bbbaaababa" or not.
($S \rightarrow bS|A$, $A \rightarrow aA|aAa|B$, $B \rightarrow bBb|A$)

The first, enumerate the rules:

1) $S \rightarrow bS$ 2) $S \rightarrow A$ 3) $A \rightarrow aA$ 4) $A \rightarrow aAa$ 5) $A \rightarrow B$ 6) $B \rightarrow bBb$ 7) $B \rightarrow A$

The second, start with initial variable S

1 1 1 2 3 3 4 5
 $S \rightarrow bS \rightarrow bbS \rightarrow bbbS \rightarrow bbbA \rightarrow bbbAa \rightarrow bbbAaA \rightarrow bbbAaAa \rightarrow bbbAaAaA$

6 7 3
 $\rightarrow bbbAaAaAbBba \rightarrow bbbAaAaAbAba \rightarrow bbbAaAaAbaAba$

We could produce it, but since there is not a stop rule, we cannot stop the system. So it is not an absolute solution.

2. (50P) According to grammar below, write PDA functions down.
($S \rightarrow AB|\epsilon$, $A \rightarrow a|AB|AA$, $B \rightarrow b|BA$)

The first, enumerate the rules:

R1) $S \rightarrow AB$ R2) $S \rightarrow \epsilon$ R3) $A \rightarrow a$ R4) $A \rightarrow AB$ R5) $A \rightarrow AA$ R6) $B \rightarrow b$ R7) $B \rightarrow BA$

According to the first type of rules ($X \rightarrow XY$)

$qa\$ \rightarrow qNBA$ for R1
 $qb\$ \rightarrow qNBA$ for R1
 $qaA \rightarrow qNBA$ for R4
 $qbA \rightarrow qNBA$ for R4
 $qaA \rightarrow qNAA$ for R5
 $qbA \rightarrow qNAA$ for R5
 $qaB \rightarrow qNAB$ for R7
 $qbB \rightarrow qNAB$ for R7

According to the second type of rules ($X \rightarrow x$)

$qaA \rightarrow qR\epsilon$ for R3
 $qbB \rightarrow qR\epsilon$ for R6

According to the third type of rules ($S \rightarrow \epsilon$)

$q\#\$ \rightarrow qN\epsilon$ for R2